

# Związki między funkcjami termodynamicznymi

Pochodna funkcji względem temperatury

$$C_V = \left( \frac{\partial U}{\partial T} \right)_{V, \zeta} \qquad \frac{C_V}{T} = \left( \frac{\partial S}{\partial T} \right)_{V, \zeta}$$

$$C_p = \left( \frac{\partial H}{\partial T} \right)_{p, \zeta} \qquad \frac{C_p}{T} = \left( \frac{\partial S}{\partial T} \right)_{p, \zeta}$$

$$-S = \left( \frac{\partial F}{\partial T} \right)_{V, \zeta} \qquad -S = \left( \frac{\partial G}{\partial T} \right)_{p, \zeta}$$

$$\Delta S_{r(V)} = \left( \frac{\partial A}{\partial T} \right)_{V, \zeta} \qquad \Delta S_{r(p)} = \left( \frac{\partial A}{\partial T} \right)_{p, \zeta}$$

Pochodna funkcji względem objętości i ciśnienia

$$\left( \frac{\partial U}{\partial V} \right)_{T, \zeta} = -p + T \left( \frac{\partial p}{\partial T} \right)_{V, \zeta} \qquad \left( \frac{\partial S}{\partial p} \right)_{T, \zeta} = - \left( \frac{\partial V}{\partial T} \right)_{p, \zeta}$$

$$\left( \frac{\partial H}{\partial p} \right)_{T, \zeta} = V - T \left( \frac{\partial V}{\partial T} \right)_{p, \zeta} \qquad \left( \frac{\partial F}{\partial V} \right)_{T, \zeta} = -p$$

$$\left( \frac{\partial S}{\partial V} \right)_{T, \zeta} = \left( \frac{\partial p}{\partial T} \right)_{V, \zeta} \qquad \left( \frac{\partial G}{\partial p} \right)_{T, \zeta} = V$$

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Pochodna funkcji względem liczby postępu reakcji

$$\begin{aligned} \left(\frac{\partial U}{\partial \zeta}\right)_{v,T} &= \Delta U_r & \left(\frac{\partial F}{\partial \zeta}\right)_{v,T} &= -A \\ \left(\frac{\partial H}{\partial \zeta}\right)_{p,T} &= \Delta H_r & \left(\frac{\partial G}{\partial \zeta}\right)_{p,T} &= -A \\ \left(\frac{\partial S}{\partial \zeta}\right)_{v,T} &= \Delta S_r & & \end{aligned}$$

$$H = U + pV$$

$$F = U - TS$$

$$H = G - T \left(\frac{\partial G}{\partial T}\right)_{p,\zeta}$$

$$A = T \left(\frac{\partial S}{\partial \zeta}\right)_{T,p} - \left(\frac{\partial H}{\partial \zeta}\right)_{T,p} = T\Delta S_r - \Delta H_r = -\Delta G_r$$